

PKU Globex Julmester

Applied Analysis for Engineering Sciences (3 Credits)

工程科学应用分析
(Course Code: 00333148)

Instructor	Emily TIAN, Wright State University (mei.tian@wright.edu) TANG Shaoqiang, Peking University (maotang@pku.edu.cn)	
Synopsis	The objectives of this course include: to show mathematical methods that are widely used in engineering sciences; to explore linear and nonlinear differential equations; to help bridge the gap between mathematical tools and physical understandings.	
Audience	Year 2+ Undergraduate and Graduate Students <u>Prerequisites</u> : Calculus (Single variate, and multi-variate), Linear Algebra.	
Classroom	TBA	
Schedule	<u>Class</u> : 9-12 AM, M-F, June 30 – July 18, 2025	<u>Total Contact Hours</u> : 45
Topics	<div>1. Recap: how to solve Ordinary Differential Equations (ODEs) exactly?<div>a) Linear ODEs with constant coefficients</div>b) General ODEs: inhomogeneous, variable coefficients, power series and perturbation method</div> <div>2. Qualitative theory of ODEs<div>a) Plane analysis for second order ODE</div>b) Stability analysis via Lyapunov function</div> c) Bifurcation and chaos <div>3. Solving PDEs: linear and nonlinear<div>a) Laplace equation: separating variables, Green’s function (* spherical and cylindrical coordinates)</div>b) Heat equation: Fourier transform, Green’s function</div> c) Wave equation: characteristic method, D’Alembert’s principled) Nonlinear equations: Burgers’ equation via Cole-Hopf transform, shock and rarefaction waves in inviscid Burgers’ equation (* traveling waves)	
Grading	<div>Homework Assignments 40%</div> <div>Exam (open-book) 60%</div> <div>Total 100%</div>	